

Integration Technique - Substitution

www.mymathscloud.com

Questions in past papers often come up combined with other topics.
Topic tags have been given for each question to enable you to know if you can do the question or whether you need to wait to cover the additional topic(s).

Scan the QR code(s) or click the link for instant detailed model solutions!

Question 1

Qualification: AP Calculus AB

Areas: Limits and Continuity, Applications of Differentiation, Differentiation, Integration

Subtopics: Differentiation Technique – Chain Rule, Differentiation Technique – Standard Functions, Tangents To Curves, Continuities and Discontinuities, Integration Technique – Substitution

Paper: Part B-Non-Calc / Series: 2012 / Difficulty: Medium / Question Number: 4

4. The function f is defined by $f(x) = \sqrt{25 - x^2}$ for $-5 \leq x \leq 5$.

(a) Find $f'(x)$.

(b) Write an equation for the line tangent to the graph of f at $x = -3$.

(c) Let g be the function defined by $g(x) = \begin{cases} f(x) & \text{for } -5 \leq x \leq -3 \\ x + 7 & \text{for } -3 < x \leq 5. \end{cases}$

Is g continuous at $x = -3$? Use the definition of continuity to explain your answer.

(d) Find the value of $\int_0^5 x\sqrt{25 - x^2} \, dx$.

SCAN ME!



Mark Scheme

[View Online](#)

SCAN ME!



Written Mark Scheme

[View Online](#)

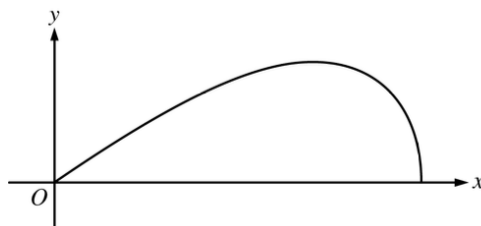
Question 2

Qualification: AP Calculus AB

Areas: Applications of Differentiation, Applications of Integration, Integration

Subtopics: Integration - Area Under A Curve, Integration Technique – Substitution, Local or Relative Minima and Maxima, Volume of Revolution – Disc Method

Paper: Part B-Non-Calc / Series: 2021 / Difficulty: Medium / Question Number: 3



3. A company designs spinning toys using the family of functions $y = cx\sqrt{4 - x^2}$, where c is a positive constant. The figure above shows the region in the first quadrant bounded by the x -axis and the graph of $y = cx\sqrt{4 - x^2}$, for some c . Each spinning toy is in the shape of the solid generated when such a region is revolved about the x -axis. Both x and y are measured in inches.
- (a) Find the area of the region in the first quadrant bounded by the x -axis and the graph of $y = cx\sqrt{4 - x^2}$ for $c = 6$.
- (b) It is known that, for $y = cx\sqrt{4 - x^2}$, $\frac{dy}{dx} = \frac{c(4 - 2x^2)}{\sqrt{4 - x^2}}$. For a particular spinning toy, the radius of the largest cross-sectional circular slice is 1.2 inches. What is the value of c for this spinning toy?
- (c) For another spinning toy, the volume is 2π cubic inches. What is the value of c for this spinning toy?

SCAN ME!



Mark Scheme

[View Online](#)

SCAN ME!



Written Mark Scheme

[View Online](#)